LOCAL SPREADING RATE ESTIMATION IN FORCED PLUMES

BY

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INSPIRATION: ORIGIN OF THE IDEA

Many years ago, Professor J. M. Redondo suggested to us that the entrainment coefficient was not constant.



IN MEMORY AND GRATITUDE

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1. INTRODUCTION

The study we present offers insights into the complex dynamics of forced turbulent plumes which are turbulent flows driven by both momentum and buoyancy fluxes.

These flows have significant geophysical importance, influencing dispersion processes in various natural and anthropogenic scenarios: volcanic eruptions, river plumes, ventilation systems or industrial emissions.

The analysis of these flows began with Morton et al. (1956), and all the studies aimed to determine the entrainment coefficient, a key parameter characterizing the rate of ambient fluid entrainment into the plume. Different studies reported varied values for the entrainment coefficient, indicating its sensitivity to experimental conditions and plume characteristics (like local turbulence production, source conditions, and distance from the source).

GENERAL OBJECTIVE

A deepen research of the entrainment process in plumes by using the spreading rate. SPECIFIC OBJECTIVES

01. To answer the question: What can we do if we want to obtain information from a geophysical phenomenon, such as a volcanic or submarine plume?

02.

To present a new methodology for analyzing plumes using image processing.

To introduce the concept of local spreading rate coefficient.



04To analyze the time

and spatial evolution of the local spreading rate coefficient.

2. LOCAL SPREADING RATE COEFFICIENT

The entrainment coefficient hypothesis (Morton et al., 1956) globally represent turbulence in plumes by introducing a constant coefficient α_E which defines the horizontal rate of surrounding fluid (entrainment velocity, U_{E} ,) in terms of the vertical velocity, W:

 $\alpha e = \frac{Ue}{W}$

The entrainment coefficient is difficult to be theoretically predicted and must be deduced from laboratory or field measurements.

For this reason, other researchers study entrainment dynamics of a plume through the spreading rate, β .



2. LOCAL SPREADING RATE COEFFICIENT

Classical and Local Spreading Rate In a stationary ambient fluid, the Spreading Rate, β , is defined as the instantaneous rate of change of plume width, *w*, relative to height *z*, for each time or frame (the linear increase of plume width, *w*, relative to distance from the source, *z*):

Classical Spreading Rate

$$\beta_{clásico} = \frac{w_{\max}}{z_{\max}}$$

It is the quotient between the maximum width and the maximum length of the plume and it globally represents the turbulent behavior of the plume. *wi* is the width of the plume corresponding to each height *zi* at a given time (as many values as heights *zi*).
Spatial and time map of the local spreading rate.
The local spreading rate represents a percentage of the classical spreading rate at the chosen height.

Local Spreading Rate

$$B_{local} = \frac{W_i}{Z_{max}}$$

3. EXPERIMENTAL SET-UP



A detailed description of the experimental set-up can be found in López, Cano and Redondo (2008) and in López et al. (2017).

Outline of the experimental procedure

We outline the experimental setup for generating a turbulent forced plume in a uniform and quiet ambient fluid. The source orifice was circular with an inner diameter d = 0.6 cm and was located at a height Ho=2 cm. The turbulent plumes were produced by pumping vertically down a potassium permanganate solution of density ρ D and volume 500 cm3. This denser fluid was discharged from the nozzle continuously at a flow rate of 8.40 cm3 s-1 into a glass tank containing fresh water of density ρ L=1 gcm-3 at a height of 16.5 cm (height of the lighter layer, hL). The Reynolds number at the source, based on the source diameter and the mean velocity there, is approximately 2000.

The salt solution had an intense purple colour and acted as a passive tracer. The flow was directly visualized being back illuminated by conventional fluorescents about 0.5 m from the tank.

The entering fluid is positively buoyant because the density of the plume fluid is greater than the ambient one and this unstable convective configuration enhances mixing. To characterize this density difference, we used the Atwood number, which is an indirect measure of the buoyancy. We used two different values for our experiments. A=0.001 and A=0.010.

3. EXPERIMENTAL SET-UP Time evolution of a plume



The flow was captured at a rate of 100 frames per second using a high-quality digital video system. The video data was organized using frame-sequencer software (VirtualDubMod), with each frame being 640x480 pixels, covering an area of 25x18 cm². Intensity values for each frame ranged from 0 to 255.

Time evolution of a plume occurring when a fluid with different density is injected into the ambient fluid for the following times: (a) 0.02 s (b) 0.07 s (c) 0.13 s (d) 0.28 s (e) 0.34 s (f) 0.38 s (g) 0.40 s (h) 0.42 s and for Atwood number A = 0.01 and height $H_o = 2 \text{ cm}$. The governing magnitudes in the plume where W is the axial or vertical velocity, r is the plume radius and U_e is the radial entrainment velocity at which the ambient fluid is coming into the plume.

4. METHODOLOGY FOR ANALYZING PLUMES USING IMAGE PROCESSING

A. MEASUREMENT PROCEDURE



Unified Matrix Type 1: the columns are the measurements of the plume length corresponding to each frame and each x-coordinate.

05.

Unified Matrix Type 2: the columns are the measurements of the plume width corresponding to each frame and each z-coordinate.



6

Otsu Method

	-					~		M	~				~	*		w		-		
	0	0	0	0	0	0	0	0	0	0	0	a	•	0	0	0	0	0	0	
	0	0	0		a	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0	0	0	0	a	0	0	0	0	0	0	a	0	0	0	0	0	0	0	
	0	0	0	0	0	•	0	0	0	0	0	0	•	0	•	0	0	0	0	
	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0	0	0	0		0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0	0		0	a	0	•	0	•	0	0	a	0	•	0	a	0	0	0	
	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	.0	0	0	
	6	2	0	3	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	
	. 9	0	0	10	0	=	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0	1	15	0	0	4	0	0	0	0	0	0	0	0	0	0	0	0	0	
	10	16	0	2	9	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	255	0	0	5	0		0	0	0	0	0	0	0	0	0	0	0	0	0	
	249	9	0	13	5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	246	6	0	0	0	7	0	0	0	0	0	0	0	0	0	0	0	0	0	
	255	0	6	7	.4	0	0	0	0	0	0	0	0	0	0	0	0	0		1
	255	255	0	0	17	0	3	1	0	11	0	0	4	0	0	0	4	249	255	
	240	255	15	0	0	0	0	0	2	11	16	0	10	0		0	255	255	2.53	
	255	237	246	255	0	11	0	13	0	0	0	7	0	0	1	0	255	240	255	
	255	255	2.52	255	240	0	D	3	6		0		0	255	255	255	255	255	255	
	254	255	255	238	255	249	10	0	0	245	255	247	255	247	251	255	255	244	255	
	255	251	247	255	245	244	244	255	255	255	252	251	248	247	255	248	255	241	255	
	242	255	248	255	250	255	255	249	250	238	255	255	253	255	245	255	255	255	243	
L	255	255	245	255	248	252	247	255	255	255	248	255	247	255	255	245	251	255	247	
1	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	
	255	255	255	255	255	255	255	255	255	255	255.	255	255	255	255	255	255	255	255	
	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	
	255	255	255	255	255	255	255	2.55	255	255	255	255	255	255	255	255	255	255	255	
	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	
	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	
	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	
	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	
	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	255	

Numerical matrix associated to a frame (one image every 0.01 s)

 Radial Profile
 Image: Constraint of the second second



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4. METHODOLOGY FOR ANALYZING PLUMES PROCESSING B. AXIAL AND RADIAL PROFILES

Unified matrix Type 1

x	F93	F94	 F135	F136
92	0	0	 52	51
93	0	0	52	54
94	0	0	55	54
95	0	0	58	60
96	0	0	53	53
97	0	0	53	51
98	0	0	54	47
99	0	0	53	49
100	0	0	49	44
101	0	0	46	49
102	0	0	53	57
103	0	0	63	57
104	0	0	58	61
105	0	0	74	69
106	0	0	73	74
107	0	0	76	78
108	0	0	71	80
109	0	0	88	82
110	0	0	87	89
111	0	0	90	91
112	0	0	92	95
113	0	0	120	146

The radial profile illustrates how the length of a plume changes along the radial x-coordinate at a constant height (z=z1) for each time.

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4. METHODOLOGY FOR ANALYZING PLUMES PROCESSING B. AXIAL AND RADIAL PROFILES

Unified matrix Type 2

The axial profile depicts the vertical variation of the plume's width relative to the vertical z-coordinate. with x=x1 fixed, for each time.







	F95	F111	F112	F113	F114
10	18	 18	18	15	13
11	20	21	20	17	16
11	21	23	21	18	19
7	20	20	26	20	23
10	19	25	25	22	17
7	20	25	23	22	24
5	19	30	25	21	15
5	18	25	27	22	21
5	15	28	26	26	32
6	14	26	29	29	29
5	13	24	29	25	29
5	10	30	25	24	27
4	12	25	24	23	29
З	12	27	22	26	30
5	14	25	29	24	30
5	13	28	23	24	28
4	14	29	31	29	28
6	13	28	29	30	28
4	14	27	32	33	30
8	13	29	32	32	27
6	14	32	30	31	27
6	16	31	36	29	30

4. METHODOLOGY FOR ANALYZING PLUMES USING IMAGE PROCESSING

Unified Matrix Type 2

Z	F102	F103	F104	F105	F106			t (s)	0,000	0,010	0,020	0,030	0,040	0,050	0,060
1	13	13	25	28	28	Zadi	n	7	F102	E103	F104	E105	E106	F107	E108
2	10	10	28	26	26		 10375	-	1 0.022	0.000	+91 I	0.021	1000	100	0.015
3	10	10	25	25	25	U,			0,022	0,022	0,024	0,021	0,021	0,014	0,015
4	12	12	27	28	28	0,	0(43	i	2 0,017	0,016	0,027	0,019	0,019	0,014	0,014
5	12	12	26	28	28	0	01124		3 0,017	0,017	0,024	0,018	0,018	0,014	0,013
6	11	11	29	29	29	0,)1498		0,021	0,021	0,026	0,021	0,021	0,014	0,014
7	12	12	26	28	28	0.	01873		0.021	0.021	0.025	0.021	0.021	0.015	0.014
8	10	10	28	32	32	0	7 100		0.019	0.019	0.028	0.021	0.021	0.017	0.014
8	10	10	17	32	32				0,010	0,010	0,020	0,021	0,021	0,011	0,014
10	3	3	20	23	23	U,U	2622		r 0,021	0,021	0,025	0,021	0,021	0,016	0,015
11	I	I	10	21	21	0,0	2996	i	8 0,017	0,017	0,027	0,024	0,024	0,017	0,015
12	9	 	16	05 ac	20	0,	03371		9 0,017	0,017	0,016	0,024	0,024	0,017	0,017
1.5	8	8	18	05 AC	05 AC	0.)3745	1	0,016	0,016	0,019	0,021	0,021	0,017	0,014
15	10	10	16	26	26		0412	•	1 0.012	0.012	0.016	0.020	0.020	0.015	0.015
16	7	 7	17	27	27		AN AN	4.	0.016	0.016	0.016	0.019	0.019	0.016	0.015
17	4	4	18	29	29		4404	li	0,010	0,010	0,010	0,010	0,010	0,010	0,015
18	0	0	16	26	26	U,I	4863];	s 0,016	0,016	0,016	0,019	0,013	0,016	0,014
19	0	0	17	27	27	0,1	5243	1.	4 0,014	0,014	0,017	0,019	0,019	0,016	0,013
20	0	0	17	27	27	0,	05618	1	5 0,017	0,017	0,016	0,019	0,019	0,015	0,014
21	1	1	14	29	29	0.0	5993	1	0.012	0.012	0.016	0.020	0.020	0.014	0.013
22	0	0	17	27	27		6367	1	7 0.007	0.007	0.017	0.021	0.021	0.015	0.014
23	0	0	17	28	28	0,	-0001	1	0,001	0,001	0,011	0,021	0,061	0,015	0,014
24	0	0	16	27	27	U,1	0142	l	0,000	0,000	0,016	0,013	0,013	0,011	0,015
25	0	0	11	24	24	0	07116	1:	9 0,000	0,000	0,016	0,020	0,020	0,017	0,015
26	0	0	10	24	24	0,	07491	21	0,000	0,000	0,016	0,020	0,020	0,016	0,015
27	0	0	9	21	21	<u> </u>	17865	_2	1 0.002	0.002	0.014	0.021	0.021	0.015	0.015
28	0	0	6	22	22	And Ballion									

Maximum width and maximum length

max w	idth	13	13	23	32	32	33	39
max a		18	18	32	42	42	56	62
alph_/	Ania	0,72	0,72	0,91	0,76	0,76	0,59	0,63
max w	idth	0,10	0,10	0,23	0,25	0,25	0,26	0,30
max z		0,07	0,07	0,12	0,16	0,16	0,21	0,23
t adimensional		0,00	0,02	0,03	0,05	0,06	0,08	0,10

 $\beta_{local} = \frac{w_i}{z_{max}} \rightarrow \beta_{local} = 0.031 \frac{n^{\circ} pixels_{black}}{z_{max}}$

C. CALCULATION OF THE LOCAL SPREADING RATE COEFFICIENT

Spreading rate Matrix

Depth Effect Correction Coefficient



A NON-INTRUSIVE 1. ANALYSIS OF PLUME DYNAMICS THAT CAN BE USED IN COMPLICATED GEOPHYSICAL PHENOMENA



COMPREHENSIVE 2. MEASUREMENTS ACROSS THE AXIAL AND RADIAL EXTENTS OF THE PLUME

A NOVEL APPROACH TO 3. STUDYING SPATIAL EVOLUTION OF THE SPREADING RATE

5. RESULTS: APPLICATIONS A. TIME EVOLUTION OF LOCAL SPREADING RATE COEFFICIENT Different time behavior depending on the zone of the plume, i.e. the axial coordinate.



From z=1 to z=111 pixels: Typical time decrease in increasing depth (z): the 1st half of the plume length.

Blocal NON CONSTANT

- **Time Dependence**
- **Axial Dependence**

From z=175 to z=250 pixels: Strong initial growth, which **4.** Final Behavior Type: is maintained as z grows and the zone of decrease the Shifting of returns. towards lower curves values of Blocal.

Figure clearly shows the existence of 4 areas with different behaviors when **1. Behavior Type 1: Classic** - Depths: z = 1 pixel to z = **111** pixels

2. Transition:

- At z = 112 pixels: Different behavior observed to z=150 pixels

3. Behavior Type 2: - Depth: z = 150 pixels to z = 175 pixels

- Depths: z = 175 pixels to z = 200 pixels

5. RESULTS: APPLICATIONS A. TIME EVOLUTION OF LOCAL SPREADING RATE COEFFICIENT

- The initial behavior is the typical decrease over time of βlocal.
- This behavior occurs within the first 1/4 of the plume length.
- The variability in βlocal values at early times may arise from both experimental uncertainties plume dynamics. and There greater are fluctuations in the plume's concentration field near its source. With time, the concentration field becomes more uniform due to diffusion, causing decrease and βlocal to approach an asymptotic far downstream, value consistent with previous studies.



- In Figure, distinct behavior is observed compared to previous depths.
- For A=0.001 (Fig. 12(a)), thelocalspreadingratecoefficientexhibitsanintensegrowthregionuntilreachingapeak,withsubsequentsmallersmallerdecreasezone,andβlocaldoesnotdecreaseassignificantly.significantly.significantly.

Fig. 9 Non-dimensional time evolution of the local spreading rate coefficient β_{local} at different lengtl (between *z*=1 *pixel* and *z*=100 *pixels*) for experiment with H_0 = 2 cm and (a) A = 0.001 (b) A = 0.01



Fig. 12 Non-dimensional time evolution of the local spreading rate β_{local} between z=150 pixels and z=175 pixels for experiment with $H_o=2$ cm and (a) A = 0.001 (b) A = 0.01

5. RESULTS: APPLICATIONS A. AXIAL EVOLUTION OF LOCAL SPREADING RATE COEFFICIENT

01.

The evolution of forced plumes is characterized by two distinct stages, as evidenced by various studies (Turner, 1973; Morton, 1959a and 1959b; Papanicolau and List, 1988; Wang and Law, 2002). Initially, forced plumes exhibit jet-like behavior, governed by momentum flux, before transitioning to plume-like behavior dominated by buoyancy.



Dong Kim et al. J. Fluid Mech. (2022), vol. 941, A42 z/Lm,

In the presented plume experiments, z/Lm spans from 0.165 to 1.879, indicating a transition from pure jet-like to forced plume behavior as the fluid flow's dynamical behavior is altered.

Various non-dimensional parameters, such as where Lm Fischer's represents characteristic length, are employed to discern whether a forced plume showcases jet-like or plume-like behavior. Typically, a forced plume is classified as a pure jet when z/Lm<0.5 and as a pure plume when z/Lm>5, with a transitional phase in between.

02.

5. RESULTS: APPLICATIONS A. AXIAL EVOLUTION OF LOCAL SPREADING RATE COEFFICIENT This approach utilizes axial profiles where the vertical coordinate z is normalized by dividing it by the maximum depth

zmax of the experimentally generated plume.

This transition is evident in the figure, depicting a shift from jet-like characteristics near the source to plume-like attributes further away, as indicated by the local spreading rate.

Figure shows all the axial profiles of *βlocal* as a function of the dimensionless depth for all times (frames) of the plume generated with A=0.001. Each curve corresponds to a time.

More specifically, there seems to be a zone of increase to the central band for both Atwood numbers and, subsequently, a decrease in the β local values .





5. RESULTS: APPLICATIONS A. AXIAL EVOLUTION OF LOCAL SPREADING RATE COEFFICIENT

To better understand where the transition from jet to plume takes place, we separate the curves corresponding to different frames in separate graphs. Figure below shows the non-dimensional vertical profiles of the local spreading rate for A=0.001 and the first half of the frames, between frames 97 and 110. :

It starts with an initial increase, the value of βlocal reaches a zone of more constant values and, later, it begins to decrease remarkably until it disappears (no existence of the plume).

This behavior implies that the local spreading rate coefficient, in addition to not being constant, presents its highest values in the central zone of the profile, with a plateau shape, which corresponds to the region of maximum width



5. RESULTS: APPLICATIONS A. AXIAL EVOLUTION OF LOCAL SPREADING RATE COEFFICIENT

To better understand where the transition from jet to plume takes place, we separate the curves corresponding to different frames in separate graphs. Figure below shows the non-dimensional vertical profiles of the local spreading rate for A=0.001 and for the second half of the frames, approximately, between frames 120 and 159:

It is observed that, again, the local coefficient β local varies with the dimensionless depth z/zmax, but a different behavior.

Figure shows a clear region where βlocal growths homogeneously for all times up to dimensionless depth of the order 0.4-0.5. From this depth, the growth is different for each curve or time, until the local spreading rate reaches a maximum. Following this, it begins to decrease rapidly and homogeneously for all times.



6. CONCLUSIONS

01.

Introduction of a novel methodology for analyzing the behavior of turbulent axisymmetric plumes using image data.

02.

Introduction of the local spreading rate to analyze the entrainment process, particularly its time and spatial evolutions.

03.

> The study reveals that spreading the rate coefficient is not constant, and, therefore, neither the is entrainment coefficient. > The study confirms the variability of entrainment with distance from the source and over time.



04.

Advantages of the new methodology:

non-invasive method of application, ▶ ease video requiring only recordings of fluid flows \triangleright applicable to geophysical and anthropogenic flows (volcanic or pollution plumes)

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